

# Multivariate Markov Chain Methods in Health Care

## CHALLENGES

### Monitoring and cost optimisation

#### The Industrial Problem

Consulting companies in healthcare and health-economics are often faced with the problem of finding cost efficient therapies and therapeutic regimens and comparing them. These challenges also emerged and need to be solved at the Healthware Consulting Ltd., Budapest.

## INDUSTRIAL SECTOR: HEALTHCARE AND HEALTH-ECONOMICS CONSULTING

### Markov-chain methods

Research



Young Research Group for developing Multivariate Markov-chain methods in monitoring health-care processes



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Simulations, cost estimation and optimisation using Markov chains with the help of custom-developed programs written in R and C++.

### Healthware Consulting Ltd.

Company



The Healthware Consulting Ltd. was founded in 2004 by with health care and health economy professionals. Over the years, due to the continuous development, the company has become a recognized health-economic consulting company in Hungary.

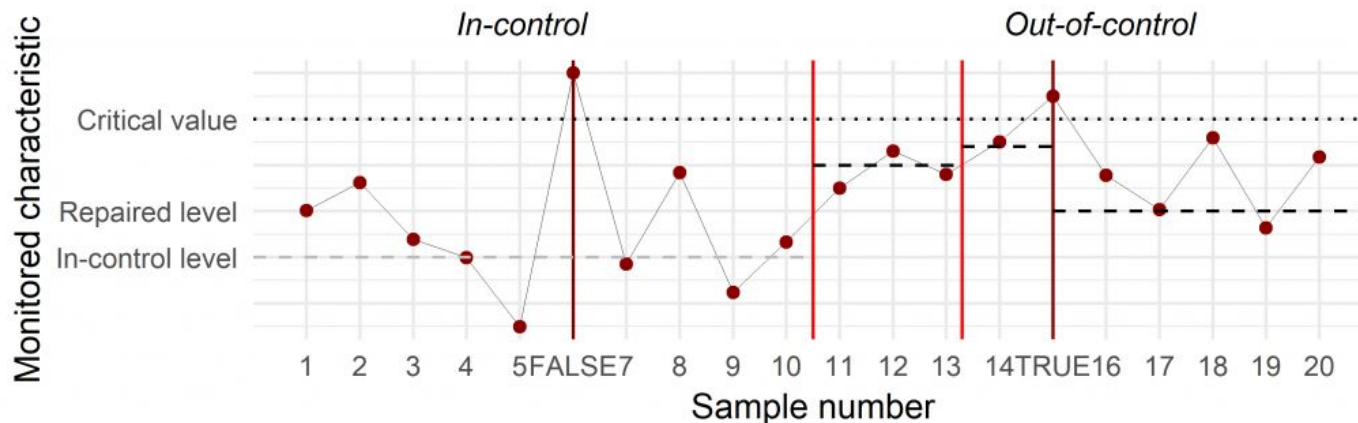
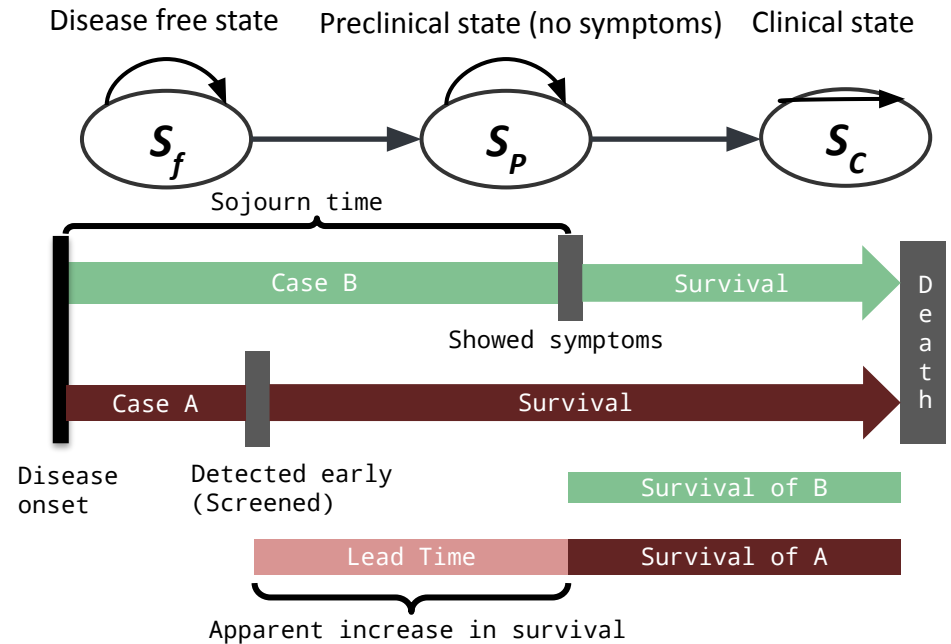


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## Challenges & Goals

- To develop **cost-optimisation** methods, which are applicable to different **medical processes**
- To incorporate the mathematical methods into a **comprehensive R package**
- To study the **performance** of the of the **convolution based disease progression model** and investigate the **identifiability** of the parameters

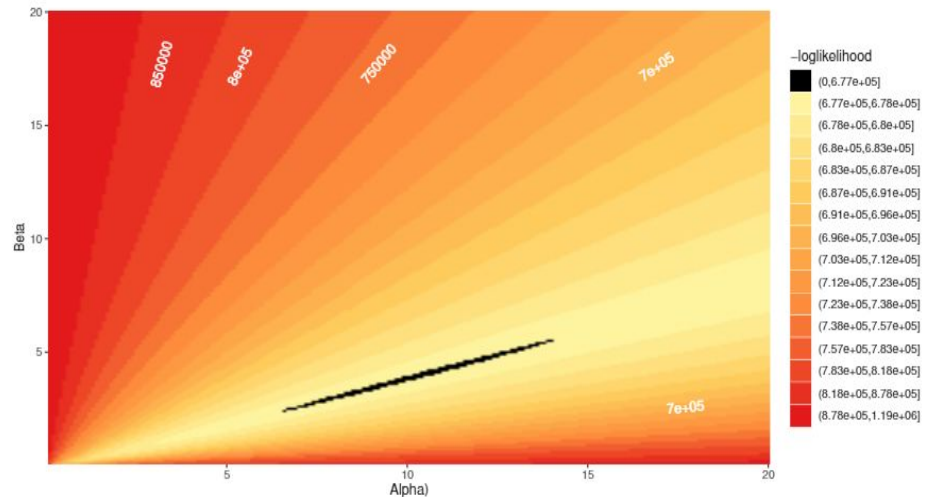
### Chronic disease progression:



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## Mathematical and computational methods and techniques applied

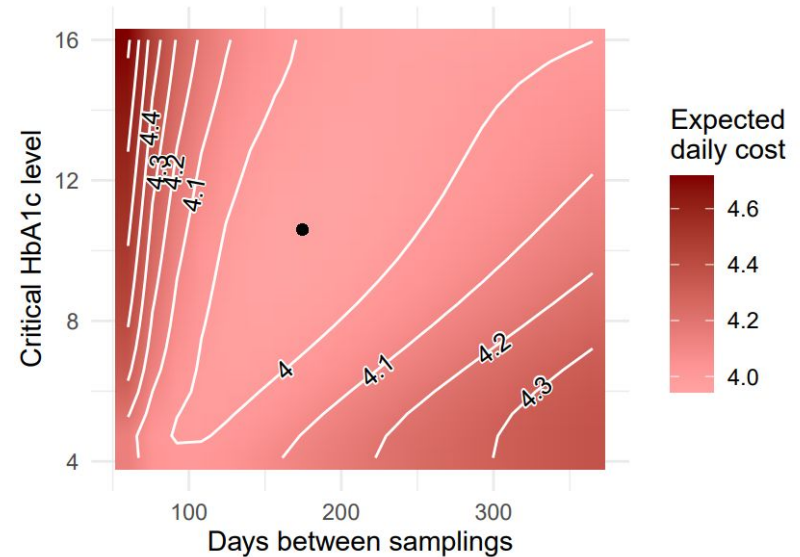
- **Simulation** of disease progression as using different **parameterizations** to study its **performance**
- New Markov chain-based control chart methods for **continuous treatment cost modelling** by a modified, highly parametrizable cost function
- Implementation of results into **R**
- New methods to investigate the **identifiability** of the parameters of convolutions of random variables
- Exposed the sensitivity of **classic** disease progression models to the underlying **assumptions**



*Contour plot of the  $-\log\text{likelihood}$  under the classical convolution based model for a gamma distributed sojourn time with parameters  $\alpha$  and  $\beta$ , the confidence region is in black*

## Results & Benefits to the company

- Powerful **simulator** of disease progression and screening programs
- Useful **methods** for proving **identifiability** in convolution setups
- Publication of the updated **Markovchart R package** on the Comprehensive R Archive Network
- Successful application of the **Markovchart package** to real-world medical data
- The results were presented at a **conference** (together with the Healthware Consulting Ltd.)
- **One new publication, one submitted manuscript and one completed manuscript**



*Contour plot of expected costs (EUR) related to insulin analogue therapy; HbA1c: glycated haemoglobin (blood sugar) level.*

**The industry has powerful simulators and R programs to estimate parameters and optimize costs**